

# Package ‘zmctp’

April 3, 2026

**Type** Package

**Title** Zero-Modified Complex 'Tri-Parametric' Pearson Distribution for Overdispersed Count Data

**Version** 0.1.0

**Description** Implements zero-modified versions of the Complex 'Tri-Parametric' Pearson distribution for overdispersed count data. The package addresses limitations of existing implementations when the parameter  $b$  approaches zero. It provides distribution functions, maximum likelihood estimation, and diagnostic tools for modeling count data with excess zeros. The methodology is based on 'Rodriguez-Avi' and coauthors (2003) <[doi:10.1007/s00362-002-0134-7](https://doi.org/10.1007/s00362-002-0134-7)>.

**License** GPL-3

**Encoding** UTF-8

**Depends** R (>= 3.5.0)

**Imports** stats, graphics

**Suggests** testthat (>= 3.0.0), knitr, rmarkdown, spelling

**VignetteBuilder** knitr

**RoxygenNote** 7.3.3

**URL** <https://github.com/roladoja/zmctp>

**BugReports** <https://github.com/roladoja/zmctp/issues>

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**Language** en-US

**NeedsCompilation** no

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**Repository** CRAN

**Date/Publication** 2026-04-03 08:00:02 UTC

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 zmctp-package

*zmctp: Zero-Modified Complex Triparametric Pearson Distribution*


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## Description

The `zmctp` package extends the Complex Triparametric Pearson (CTP) distribution with zero-modified versions for handling overdispersed count data, particularly when the parameter  $b$  approaches zero.

## Details

Main functions:

- `dctp`, `pctp`, `qctp`, `rctp` - CTP distribution functions
- `dzictp`, `pzictp`, `qzictp`, `rzictp` - Zero-Modified CTP distribution functions
- `ctp.fit` - Fit CTP model
- `zictp.fit` - Fit Zero-Modified CTP model

## Author(s)

**Maintainer:** Rasheedat Oladoja <roladoja@ttu.edu> ([ORCID](#))

**See Also**

Useful links:

- <https://github.com/roladoja/zmctp>
- Report bugs at <https://github.com/roladoja/zmctp/issues>

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 ctp.fit

*Maximum Likelihood Estimation for the CTP Distribution*


---

**Description**

Fits the Complex Triparametric Pearson (CTP) distribution to count data using maximum likelihood estimation.

**Usage**

```
ctp.fit(
  x,
  a_start = NULL,
  b_start = NULL,
  gama_start = NULL,
  method = "L-BFGS-B",
  penalty = 1e+10
)
```

**Arguments**

x	Numeric vector of nonnegative counts.
a_start	Optional starting value for parameter a.
b_start	Optional starting value for parameter b.
gama_start	Optional starting value for parameter gamma.
method	Optimization method (default: "L-BFGS-B").
penalty	numeric penalty added for numerical stability when $b \rightarrow 0$

**Value**

An object of class "ctffit" containing:

estimates	Named vector of MLEs
se	Standard errors
vcov	Variance-covariance matrix
logLik	Log-likelihood
AIC	Akaike Information Criterion
BIC	Bayesian Information Criterion

pearson_chisq	Pearson's chi-squared statistic
wald_chisq	Wald's chi-squared statistic
fitted_freq	Data frame of observed vs expected frequencies
data	Original data
converged	Convergence status

### Examples

```
set.seed(123)

x <- rctp(30, a = 1, b = 0.5, gama = 5)
fit <- ctp.fit(x)
print(fit)
plot(fit)
```

---

dctp

---

*Probability Mass Function of the CTP Distribution*


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### Description

Evaluates the probability mass function of the Complex TriParametric Pearson (CTP) distribution for nonnegative integer values.

The pmf is

$$p(x) = p(0) \frac{(a + ib)_x (a - ib)_x}{(\gamma)_x x!}, \quad x = 0, 1, \dots$$

and satisfies the recurrence

$$\frac{p(x + 1)}{p(x)} = \frac{(a + x)^2 + b^2}{(\gamma + x)(x + 1)}.$$

### Usage

```
dctp(x, a, b, gama, log = FALSE)
```

### Arguments

x	Vector of nonnegative integers.
a	Parameter a.
b	Parameter b (must satisfy $b \geq 0$ ).
gama	Parameter gamma.
log	Logical; if TRUE, returns log-probabilities.

### Value

A numeric vector of probabilities.

**Examples**

```
dctp(0:5, a = 1, b = 0.5, gama = 6)
```

---

 dzictp
 

---



---

*Probability Mass Function of the ZM-CTP Distribution*


---

**Description**

The Zero-Modified CTP (ZM-CTP) distribution modifies the zero probability of the baseline CTP distribution.

**Usage**

```
dzictp(x, a, b, gama, omega, log = FALSE)
```

**Arguments**

x	Vector of nonnegative integers.
a	Parameter a.
b	Parameter b.
gama	Parameter gamma.
omega	Zero-modification parameter, with $0 < \omega < 1$ .
log	Logical; if TRUE, returns log-probabilities.

**Value**

Numeric vector of probabilities.

**Examples**

```
dzictp(0:5, a = 1, b = 0.5, gama = 6, omega = 0.3)
```

---

 pctp
 

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*Cumulative Distribution Function of the CTP Distribution*


---

**Description**

Cumulative Distribution Function of the CTP Distribution

**Usage**

```
pctp(q, a, b, gama, lower.tail = TRUE, log.p = FALSE)
```

**Arguments**

q	Vector of quantiles.
a	Parameter a.
b	Parameter b.
gama	Parameter gamma.
lower.tail	Logical; if TRUE, probabilities are $P(X \leq q)$ , otherwise $P(X > q)$ .
log.p	Logical; if TRUE, probabilities are given on the log scale.

**Value**

Numeric vector of cumulative probabilities.

**Examples**

```
pctp(0:5, a = 1, b = 0.5, gama = 6)
```

---

plot.ctpfit

*Plot method for ctpfit objects*

---

**Description**

Plot method for ctpfit objects

**Usage**

```
## S3 method for class 'ctpfit'
plot(x, type = c("frequency", "cdf", "qq"), ...)
```

**Arguments**

x	A ctpfit object
type	Type of plot: "frequency", "cdf", or "qq"
...	Additional graphical parameters

**Value**

No return value. Called for its side effect of producing a plot.

---

plot.zictpfit	<i>Plot method for zictpfit objects</i>
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---

**Description**

Creates diagnostic plots for Zero-Modified CTP distribution fits, including frequency comparisons, CDF plots, and Q-Q plots.

**Usage**

```
## S3 method for class 'zictpfit'  
plot(x, type = c("frequency", "cdf", "qq"), ...)
```

**Arguments**

x	A zictpfit object from zictp.fit()
type	Type of plot: "frequency", "cdf", or "qq"
...	Additional graphical parameters

**Value**

No return value. Called for its side effect of producing a plot.

---

print.ctpfit	<i>Print method for ctpfit objects</i>
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**Description**

Print method for ctpfit objects

**Usage**

```
## S3 method for class 'ctpfit'  
print(x, ...)
```

**Arguments**

x	A ctpfit object
...	Additional arguments (ignored)

**Value**

Invisibly returns the original fitted model object. The function is called for its side effect of printing a model summary.

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<code>print.zictpfit</code>	<i>Print method for zictpfit objects</i>
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**Description**

Print method for zictpfit objects

**Usage**

```
## S3 method for class 'zictpfit'
print(x, ...)
```

**Arguments**

<code>x</code>	A zictpfit object
<code>...</code>	Additional arguments (ignored)

**Value**

Invisibly returns the original fitted model object. The function is called for its side effect of printing a model summary.

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<code>pzictp</code>	<i>Cumulative Distribution Function of the ZM-CTP Distribution</i>
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---

**Description**

Cumulative Distribution Function of the ZM-CTP Distribution

**Usage**

```
pzictp(q, a, b, gama, omega, lower.tail = TRUE, log.p = FALSE)
```

**Arguments**

<code>q</code>	Vector of quantiles.
<code>a</code>	Parameter a.
<code>b</code>	Parameter b.
<code>gama</code>	Parameter gamma.
<code>omega</code>	Zero-modification parameter.
<code>lower.tail</code>	Logical.
<code>log.p</code>	Logical.

**Value**

Numeric vector of cumulative probabilities.

**Examples**

```
pzictp(0:5, a = 1, b = 0.5, gama = 6, omega = 0.3)
```

---

qctp

*Quantile Function of the CTP Distribution*


---

**Description**

Quantile Function of the CTP Distribution

**Usage**

```
qctp(p, a, b, gama, lower.tail = TRUE, log.p = FALSE, max_q = 1000)
```

**Arguments**

p	Vector of probabilities.
a	Parameter a.
b	Parameter b.
gama	Parameter gamma.
lower.tail	Logical.
log.p	Logical.
max_q	Maximum x to search.

**Value**

Numeric vector of quantiles.

**Examples**

```
qctp(c(0.25, 0.5, 0.75), a = 1, b = 0.5, gama = 6)
```

---

`qzictp`*Quantile Function of the ZM-CTP Distribution*

---

**Description**

Quantile Function of the ZM-CTP Distribution

**Usage**

```
qzictp(p, a, b, gama, omega, lower.tail = TRUE, log.p = FALSE, max_q = 1000)
```

**Arguments**

<code>p</code>	Vector of probabilities.
<code>a</code>	Parameter a.
<code>b</code>	Parameter b.
<code>gama</code>	Parameter gamma.
<code>omega</code>	Zero-modification parameter.
<code>lower.tail</code>	Logical.
<code>log.p</code>	Logical.
<code>max_q</code>	Maximum x to search.

**Value**

Numeric vector of quantiles.

**Examples**

```
qzictp(c(0.25, 0.5, 0.75), a = 1, b = 0.5, gama = 6, omega = 0.3)
```

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`rctp`*Random Generation from the CTP Distribution*

---

**Description**

Random Generation from the CTP Distribution

**Usage**

```
rctp(n, a, b, gama)
```

**Arguments**

n	Number of observations.
a	Parameter a.
b	Parameter b.
gama	Parameter gamma.

**Value**

Integer vector of random draws.

**Examples**

```
set.seed(123)
rctp(10, a = 1, b = 0.5, gama = 6)
```

---

rzictp

*Random Generation from the ZM-CTP Distribution*

---

**Description**

Random Generation from the ZM-CTP Distribution

**Usage**

```
rzictp(n, a, b, gama, omega)
```

**Arguments**

n	Number of observations.
a	Parameter a.
b	Parameter b.
gama	Parameter gamma.
omega	Zero-modification parameter.

**Value**

Integer vector of random draws.

**Examples**

```
set.seed(123)
rzictp(10, a = 1, b = 0.5, gama = 6, omega = 0.3)
```

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summary.ctpfit	<i>Summary method for ctpfit objects</i>
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**Description**

Summary method for ctpfit objects

**Usage**

```
## S3 method for class 'ctpfit'
summary(object, ...)
```

**Arguments**

object	A ctpfit object
...	Additional arguments (ignored)

**Value**

Invisibly returns the original fitted model object. The function is called for its side effects, producing a formatted summary of parameter estimates, moments, and goodness-of-fit diagnostics.

---

summary.zictpfit	<i>Summary method for zictpfit objects</i>
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**Description**

Summary method for zictpfit objects

**Usage**

```
## S3 method for class 'zictpfit'
summary(object, ...)
```

**Arguments**

object	A zictpfit object
...	Additional arguments (ignored)

**Value**

Invisibly returns the original fitted model object. The function is called for its side effects, producing a formatted summary of parameter estimates, moments, and goodness-of-fit diagnostics.

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zictp.fit	<i>Maximum Likelihood Estimation for the Zero-Modified CTP Distribution</i>
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### Description

Fits the Zero-Modified Complex TriParametric Pearson (ZM-CTP) distribution to count data using maximum likelihood estimation.

A logit reparameterization is used for omega to ensure  $0 < \omega < 1$ , and a log reparameterization is used for gamma so that  $\text{gama} = 2 \cdot a + 2 + \exp(\eta)$ , which guarantees variance existence throughout optimization.

### Usage

```
zictp.fit(
  x,
  a_start = NULL,
  b_start = NULL,
  gama_start = NULL,
  omega_start = NULL,
  method = "BFGS"
)
```

### Arguments

x	Numeric vector of nonnegative counts.
a_start	Optional starting value for parameter a.
b_start	Optional starting value for parameter b.
gama_start	Optional starting value for parameter gamma.
omega_start	Optional starting value for omega ( $0 < \omega < 1$ ).
method	Optimization method (default: "BFGS").

### Value

An object of class "zictpfit".

### Examples

```
set.seed(123)
x <- rzictp(30, a = 1, b = 0.5, gama = 5, omega = 0.3)
fit <- zictp.fit(x)
fit$estimates
```

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