

# Package ‘GammaFrailty’

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**Type** Package

**Title** Gamma Frailty Regression Models with Multiple Baseline Distributions

**Version** 0.1.0

**Description** Implements univariate gamma frailty regression models for survival data with six different baseline distributions: the Arvind distribution (Pandey et al., 2024), the Lindley distribution (Lindley, 1958), the Linear Failure Rate distribution (Bain, 1974), the Power Xgamma distribution (Tyagi et al., 2022), the Modified Topp-Leone distribution (Singh et al., 2025), and the Power Failure Rate distribution (Mugdadi, 2005). The package supports uncensored (complete) and censored data (right, left, interval, and progressive censoring) with and without covariates. It provides maximum likelihood estimation, standard errors, confidence intervals, t-statistics, p-values, Akaike Information Criterion (AIC), Bayesian Information Criterion (BIC), a bootstrap approximation of the Widely Applicable Information Criterion (WAIC), k-fold cross-validation, variance inflation factors, R-squared, adjusted R-squared, Mean Squared Error (MSE), Mean Absolute Error (MAE), Root Mean Squared Error (RMSE), an overall model F-test, frailty variance estimation, survival probabilities at user-specified time points, median survival, expected survival within a fixed window, risk predictions, marginal predictions, martingale and deviance residuals, standardized and studentized residuals, leverage values, Cook's distance, Difference in Fits (DFFITS), Difference in Betas (DFBETAS), and a comprehensive suite of diagnostic and survival plots including Kaplan-Meier overlays and coefficient forest plots. Random number generation is available for each baseline distribution and the full frailty model, and a simulation study function evaluates parameter recovery across sample sizes and censoring scenarios.

References are Lindley (1958) <[doi:10.1111/j.2517-6161.1958.tb00278.x](https://doi.org/10.1111/j.2517-6161.1958.tb00278.x)>, Mugdadi (2005) <[doi:10.1016/j.amc.2004.09.064](https://doi.org/10.1016/j.amc.2004.09.064)>, Bain (1974) <[doi:10.1080/00401706.1974.10489237](https://doi.org/10.1080/00401706.1974.10489237)>, Singh, Tyagi, Singh, and Tyagi (2025) <<https://ph02.tci-thaijo.org/index.php/thaistat/article/view/257215>>.

Pandey, Singh, Tyagi, and Tyagi (2024)  
<https://ssca.org.in/journal.html>, and  
 Tyagi, Kumar, Pandey, Saha, and Bagariya (2022)  
<https://ijsreg.com/>.

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baseline_hazard	<i>Baseline Cumulative Hazard and Hazard Functions</i>
-----------------	--

---

**Description**

Computes the baseline cumulative hazard  $H_0(t)$  and baseline hazard  $h_0(t)$  for the six supported distributions.

**Usage**

```
baseline_hazard(t, baseline, par)
```

**Arguments**

t	positive numeric vector of time points.
baseline	character; baseline distribution name. One of "arvind", "lindley", "lfr", "pvg", "mtl", "pfr".
par	numeric vector of baseline parameters (see Details).

**Details**

**Arvind** (par = c(alpha)):  $H_0(t) = \alpha t^2 + \log(1 + \alpha t)$ ,  $h_0(t) = 2\alpha t + \alpha/(1 + \alpha t)$ .

**Lindley** (par = c(lambda)):  $H_0(t) = \lambda t - \log(1 + \lambda t/(1 + \lambda))$ ,  $h_0(t) = \lambda^2(1 + t)/(1 + \lambda + \lambda t)$ .

**LFR** (par = c(a, b)):  $H_0(t) = at + bt^2/2$ ,  $h_0(t) = a + bt$ .

**Power Xgamma** (par = c(alpha, beta)):  $H_0(t) = \alpha t^{1/\beta} + \log(1 + \alpha) - \log(1 + \alpha + \alpha t^{1/\beta} + \alpha^2 t^{2/\beta}/2)$ .

**Modified Topp-Leone** (par = c(alpha)):  $H_0(t) = -\log\left(1 - \left(\frac{2t+t^2}{(1+t)^2}\right)^\alpha\right)$ .

**Power Failure Rate** (par = c(a, k)):  $H_0(t) = \frac{a}{k+1} t^{k+1}$ ,  $h_0(t) = at^k$ .

**Value**

A list with components:

**H0** Numeric vector of cumulative hazard values.

**h0** Numeric vector of hazard values.

**Examples**

```
bh <- baseline_hazard(seq(0.1, 2, by = 0.1), baseline = "arvind", par = 0.5)
plot(seq(0.1, 2, by = 0.1), bh$h0, type = "l", main = "Arvind hazard")
```

---

 bootstrap\_waic

*Bootstrap WAIC for the Gamma Frailty Model*


---

**Description**

Approximates the Widely Applicable Information Criterion (WAIC) via bootstrap re-sampling of the log-likelihood. Since the package uses frequentist MLE, this serves as a computationally tractable approximation to the Bayesian WAIC.

**Usage**

```
bootstrap_waic(fit, B = 200)
```

**Arguments**

**fit** An object of class "gamma\_frailty\_fit".

**B** integer; number of bootstrap iterations (default 200).

**Value**

A named list:

**WAIC**  $-2 \times (\text{lppd} - p_{\text{WAIC}})$ .

**lppd** Log pointwise predictive density.

**p\_waic** Effective number of parameters.

**B\_effective** Number of successful bootstrap draws used.

**Examples**

```
set.seed(1)
dat <- r_gamma_frailty(80, "arvind", par = 0.5, theta = 0.3,
  cen_type = "right")
fit <- fit_gamma_frailty(dat$time, dat$status, baseline = "arvind")
bootstrap_waic(fit, B = 50)
```

---

compare_models	<i>Compare Multiple Gamma Frailty Models</i>
----------------	--

---

**Description**

Compiles AIC, BIC, log-likelihood, frailty variance, and (optionally) WAIC for a list of fitted gamma frailty models.

**Usage**

```
compare_models(..., compute_waic = FALSE, waic_B = 100L)
```

**Arguments**

...	named objects of class "gamma_frailty_fit". Names are used as row labels in the output table. You may also pass a single named list.
compute_waic	logical; if TRUE, compute bootstrap WAIC for each model (slow; default FALSE).
waic_B	integer; bootstrap iterations for WAIC (default 100).

**Value**

A data frame with columns Baseline, logLik, K, AIC, BIC, theta, and optionally WAIC.

**Examples**

```
set.seed(8)
dat <- r_gamma_frailty(100, "arvind", par = 0.5, theta = 0.3,
  cen_type = "right")
f1 <- fit_gamma_frailty(dat$time, dat$status, baseline = "arvind")
f2 <- fit_gamma_frailty(dat$time, dat$status, baseline = "lindley")
compare_models(Arvind = f1, Lindley = f2)
```

---

cv_frailty	<i>K-Fold Cross-Validation for the Gamma Frailty Model</i>
------------	--

---

**Description**

Performs k-fold cross-validation and reports out-of-sample log-likelihood and RMSE.

**Usage**

```
cv_frailty(  
  time,  
  status,  
  x = matrix(nrow = length(time), ncol = 0),  
  baseline = "arvind",  
  k = 5L,  
  time2 = NULL  
)
```

**Arguments**

time	positive numeric vector of event/censoring times.
status	integer vector of censoring indicators.
x	numeric matrix of covariates (may have zero columns).
baseline	character; baseline distribution.
k	integer; number of folds (default 5).
time2	numeric vector; upper bound for interval-censored obs.

**Value**

A named list:

**mean\_oos\_loglik** Mean out-of-sample log-likelihood.

**sd\_oos\_loglik** Standard deviation across folds.

**mean\_oos\_rmse** Mean out-of-sample RMSE.

**sd\_oos\_rmse** SD of RMSE across folds.

**fold\_logliks, fold\_rmses** Per-fold values.

**Examples**

```
set.seed(7)  
dat <- r_gamma_frailty(120, "lfr", par = c(0.5, 0.2), theta = 0.4,  
  cen_type = "right")  
cv_frailty(dat$time, dat$status, baseline = "lfr", k = 5)
```

**Description**

Returns a consolidated data frame of all diagnostic measures for each observation, suitable for identifying outliers and influential points.

**Usage**

```
diagnostics_table(fit)
```

**Arguments**

`fit` An object of class "gamma\_frailty\_fit".

**Value**

A data frame with columns: time, status, cox\_snell, martingale, deviance, raw, standardized, studentized, leverage, cooks\_distance, DFFITS, and one column per covariate for DFBETAS.

**Examples**

```
set.seed(3)
dat <- r_gamma_frailty(60, "pfr", par = c(0.5, 1), theta = 0.3,
  cen_type = "right")
fit <- fit_gamma_frailty(dat$time, dat$status, baseline = "pfr")
diag_tbl <- diagnostics_table(fit)
head(diag_tbl)
```

---

fit\_gamma\_frailty      *Fit a Gamma Frailty Regression Model*

---

**Description**

Fits a gamma frailty regression model with the chosen baseline distribution via maximum likelihood estimation (MLE). Handles uncensored and right-, left-, interval-, and progressive-censored data, with and without covariates.

**Usage**

```
fit_gamma_frailty(
  time,
  status,
  x = matrix(nrow = length(time), ncol = 0),
  baseline = "arvind",
  time2 = NULL,
  prog_cen = NULL,
  init = NULL
)
```

**Arguments**

`time` positive numeric vector of event or censoring times.

`status` integer vector indicating the observation type: 1 = exact event, 0 = right-censored, 2 = left-censored, 3 = interval-censored.

<code>x</code>	numeric matrix or data frame of covariates. Use an empty matrix (zero columns) for a no-covariate model. Default: <code>matrix(nrow = length(time), ncol = 0)</code> .
<code>baseline</code>	character; baseline distribution. One of "arvind", "lindley", "lfr", "pxg", "mtl", "pfr".
<code>time2</code>	numeric vector; upper bound for interval-censored observations (required when any <code>status == 3</code> ).
<code>prog_cen</code>	integer vector; number of items progressively removed at the $j$ -th failure time (progressive censoring adjustment).
<code>init</code>	numeric vector of initial parameter values on the log scale for baseline parameters and log scale for $\theta$ . If NULL, sensible defaults are used.

### Value

An object of class "gamma\_frailty\_fit" (a named list) with components:

**coefficients** Data frame with columns Estimate, StdErr, t\_stat, p\_value, CI\_lower, CI\_upper, Signif.

**logLik** Maximised log-likelihood.

**AIC** Akaike Information Criterion.

**BIC** Bayesian Information Criterion.

**vcov** Variance-covariance matrix of estimates (log scale).

**baseline** Name of the baseline distribution.

**theta** Estimated frailty variance.

**theta\_se** Standard error of the frailty variance (delta method).

**VIF** Named numeric vector of variance inflation factors (when `ncol(x) > 1`).

**Tolerance** Tolerance =  $1/\text{VIF}$ .

**F\_stat** Wald F-statistic for overall covariate significance.

**p\_F\_stat** P-value for the F-statistic.

**n** Sample size.

**n\_cov** Number of covariates.

**n\_par\_base** Number of baseline parameters.

**time, status, x, time2, prog\_cen** Input data stored for post-fit diagnostics.

**raw\_est** Named numeric vector of estimates on the log/original scale used internally for prediction and diagnostics.

### Examples

```
set.seed(1)
dat <- r_gamma_frailty(100, "arvind", par = 0.5, theta = 0.3,
                      cen_type = "right", cen_rate = 0.2)
fit <- fit_gamma_frailty(dat$time, dat$status, baseline = "arvind")
summary(fit)
```

---

forecast_frailty	<i>Forecast Survival Curves</i>
------------------	---------------------------------

---

**Description**

Extends the model-based survival curve beyond the observed training range to a specified forecast horizon.

**Usage**

```
forecast_frailty(fit, horizon, n_grid = 200, newdata = NULL)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
horizon	positive numeric; the maximum time to forecast to.
n_grid	integer; number of equally spaced time points in $[0, \text{horizon}]$ to evaluate (default 200).
newdata	optional covariate matrix for new subjects.

**Value**

A list with `time` (grid of time points) and `survival` (matrix, subjects x `n_grid`).

**Examples**

```
set.seed(1)
dat <- r_gamma_frailty(80, "arvind", par = 0.5, theta = 0.3,
                      cen_type = "right")
fit <- fit_gamma_frailty(dat$time, dat$status, baseline = "arvind")
fc <- forecast_frailty(fit, horizon = 5)
plot(fc$time, fc$survival[1, ], type = "l", xlab = "Time",
      ylab = "S(t)", main = "Forecast")
```

---

gamma_frailty	<i>Gamma Frailty Regression Model (Formula Interface)</i>
---------------	---

---

**Description**

A formula-based interface to `fit_gamma_frailty`, modelled after `lm` and `glm`. The response must be a `Surv` object.

**Usage**

```
gamma_frailty(
  formula,
  data,
  baseline = "arvind",
  time2 = NULL,
  prog_cen = NULL,
  init = NULL
)
```

**Arguments**

formula	a <a href="#">formula</a> object. The left-hand side must be a <code>Surv(time, status)</code> or <code>Surv(time, time2, status, type = "interval")</code> object.
data	a data frame containing the variables in the formula.
baseline	character; baseline distribution. One of "arvind", "lindley", "lfr", "pxg", "mtl", "pfr".
time2	numeric vector; upper bound for interval-censored observations.
prog_cen	integer vector; progressive censoring scheme.
init	numeric vector; initial parameter values.

**Value**

An object of class `c("gamma_frailty", "gamma_frailty_fit")` with an additional call and formula component.

**Examples**

```
set.seed(1)
dat <- r_gamma_frailty(100, "arvind", par = 0.5, theta = 0.3,
  x = matrix(rnorm(100), ncol = 1),
  beta = 0.5, cen_type = "right", cen_rate = 0.2)
colnames(dat)[4] <- "X1"
fit <- gamma_frailty(survival::Surv(time, status) ~ X1,
  data = dat, baseline = "arvind")
summary(fit)
```

---

gamma\_frailty\_functions

*Gamma Frailty Model Functions*

---

**Description**

Computes the survival function  $S(t)$ , density  $f(t)$ , hazard  $h(t)$ , and cumulative hazard  $\mathcal{H}(t)$  for the gamma frailty model.

**Usage**

```
gamma_frailty_functions(t, eta, theta, baseline, par)
```

**Arguments**

t	positive numeric vector of time points.
eta	positive numeric vector of linear predictors $\eta_j = e^{X_j\beta}$ . Must have the same length as t or be a scalar.
theta	positive numeric; frailty variance.
baseline	character; baseline distribution name.
par	numeric vector of baseline parameters.

**Details**

The marginal survival function (after integrating out the gamma frailty) is

$$S(t_j) = [1 + \theta\eta_j H_0(t_j)]^{-1/\theta}.$$

The corresponding density, hazard, and cumulative hazard are derived analytically from this expression.

**Value**

A list with components S, f, h, H.

**Examples**

```
gf <- gamma_frailty_functions(1:5, eta = 1, theta = 0.5,
                             baseline = "arvind", par = 0.5)
plot(1:5, gf$S, type = "l", main = "Survival")
```

---

influence\_frailty      *Influence Diagnostics for the Gamma Frailty Model*

---

**Description**

Computes leverage values, Cook's distance, DFFITS, and DFBETAS for identifying outliers and influential observations.

**Usage**

```
influence_frailty(fit)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
-----	---

**Value**

A named list with components:

**leverage** Approximate hat values  $h_{ii}$ .

**std\_residuals** Standardized deviance residuals.

**stu\_residuals** Studentized deviance residuals (LOO approx).

**cooks\_distance** Cook's distance  $D_i$ .

**DFFITs** DFFITS values.

**DFBETAS** Matrix of DFBETAS, one column per covariate.

**Examples**

```
set.seed(2)
dat <- r_gamma_frailty(80, "lfr", par = c(0.5, 0.2), theta = 0.4,
                      x = matrix(rnorm(80), ncol = 1),
                      beta = 0.5, cen_type = "right")
fit <- fit_gamma_frailty(dat$time, dat$status, dat[, 4, drop = FALSE],
                        baseline = "lfr")
inf <- influence_frailty(fit)
plot(inf$cooks_distance, type = "h", main = "Cook's Distance")
```

---

loglik\_gamma\_frailty *Log-Likelihood for the Gamma Frailty Model*

---

**Description**

Internal function computing the total log-likelihood for uncensored and censored (right, left, interval, progressive) data.

**Usage**

```
loglik_gamma_frailty(
  par_all,
  time,
  status,
  x,
  baseline,
  time2 = NULL,
  prog_cen = NULL
)
```

**Arguments**

par_all	numeric vector of ALL parameters on the estimation scale (log-transformed for positivity constraints): <code>c(log(baseline_pars), beta_covariates, log(theta))</code> .
time	numeric vector of event or censoring times.
status	integer vector: 1 = exact event, 0 = right-censored, 2 = left-censored, 3 = interval-censored.
x	numeric matrix of covariates (can have zero columns).
baseline	character; baseline distribution name.
time2	numeric vector; upper bound for interval-censored observations ( <code>status == 3</code> ). Ignored otherwise.
prog_cen	integer vector; number of items progressively removed at each observed failure time. If NULL, no progressive adjustment.

**Value**

Scalar log-likelihood value (or  $-1e12$  if infeasible).

---

plot_all	<i>Plot All Diagnostics</i>
----------	-----------------------------

---

**Description**

Generates all 8 diagnostic plots for a fitted gamma frailty model and displays them in the **active R graphics device** (e.g., the RStudio Plots pane). Plots are **never** saved to a file automatically. To save, wrap the call in `pdf()` / `dev.off()` yourself, or use the `save_to_file` argument.

**Usage**

```
plot_all(fit, ask = grDevices::dev.interactive(), save_to_file = NULL)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
ask	logical; if TRUE (the default in interactive sessions) R pauses and waits for the user to press Enter before drawing each new plot. Set <code>ask = FALSE</code> to cycle through all plots without pausing.
save_to_file	character or NULL (default). If a file path is supplied (e.g., "diagnostics.pdf" or "plot.png"), the 8 plots are written to that file instead of the screen. The file type is detected from the extension (.pdf, .png, .svg, .jpeg / .jpg). When NULL (default) the plots go to the active device only.

**Value**

Invisibly returns `fit`.

**Note**

This function **never** saves plots automatically. The `save_to_file` argument exists purely for user convenience and is `NULL` by default.

**Examples**

```
set.seed(1)
dat <- r_gamma_frailty(80, "arvind", par = 0.5, theta = 0.3,
  cen_type = "right", cen_rate = 0.2)
fit <- fit_gamma_frailty(dat$time, dat$status, baseline = "arvind")
# Display all 8 plots in the R graphics window (no file saved):
plot_all(fit, ask = FALSE)
```

---

plot\_baseline

*Plot Baseline Distribution Functions*


---

**Description**

Plots the PDF, CDF, survival function, and hazard function for a specified baseline distribution over a time grid.

**Usage**

```
plot_baseline(baseline, par, t_range = c(0.01, 3), n_grid = 300)
```

**Arguments**

<code>baseline</code>	character; baseline distribution name.
<code>par</code>	numeric vector of baseline parameters.
<code>t_range</code>	numeric vector of length 2 giving the time range.
<code>n_grid</code>	integer; number of grid points (default 300).

**Value**

Invisibly returns a list with components `t` (time grid), `f` (PDF), `F` (CDF), `S` (survival), and `h` (hazard) evaluated over the time grid.

**Examples**

```
plot_baseline("arvind", par = 0.5, t_range = c(0.01, 3))
```

---

plot_coef_forest	<i>Coefficient Forest Plot</i>
------------------	--------------------------------

---

**Description**

Displays all parameter estimates with 95% confidence intervals as a horizontal forest (dot-and-whisker) plot.

**Usage**

```
plot_coef_forest(fit, ...)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
...	additional graphical parameters.

**Value**

No return value, called for side effects (plotting).

---

plot_dfbetas	<i>DFBETAS Dot Plot</i>
--------------	-------------------------

---

**Description**

Plots DFBETAS values as a stem plot for each covariate, highlighting observations that exceed the  $2/\sqrt{n}$  threshold in red.

**Usage**

```
plot_dfbetas(fit, ...)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
...	additional graphical parameters.

**Value**

No return value, called for side effects (plotting).

---

plot_leverage	<i>Leverage Histogram</i>
---------------	---------------------------

---

**Description**

Displays a histogram of leverage values with a threshold line at  $2(p + 1)/n$ .

**Usage**

```
plot_leverage(fit, ...)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
...	additional graphical parameters.

**Value**

No return value, called for side effects (plotting).

---

plot_qq_residuals	<i>Q-Q Plot of Cox-Snell Residuals</i>
-------------------	--

---

**Description**

Compares sorted Cox-Snell residuals against theoretical quantiles of the standard exponential distribution. Deviations from the diagonal indicate model misfit.

**Usage**

```
plot_qq_residuals(fit, ...)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
...	additional graphical parameters.

**Value**

No return value, called for side effects (plotting).

---

`plot_residuals_fitted` *Residuals vs Fitted Values Plot*

---

**Description**

Plots deviance residuals against fitted survival probabilities with a LOWESS smoother to assess linearity and heteroscedasticity.

**Usage**

```
plot_residuals_fitted(fit, ...)
```

**Arguments**

`fit` An object of class "gamma\_frailty\_fit".  
`...` additional graphical parameters passed to plot.

**Value**

No return value, called for side effects (plotting).

---

`plot_residuals_leverage`  
*Residuals vs Leverage Plot*

---

**Description**

Plots deviance residuals against leverage values with Cook's distance contours ( $D = 0.5$  and  $D = 1$ ) to identify influential points.

**Usage**

```
plot_residuals_leverage(fit, ...)
```

**Arguments**

`fit` An object of class "gamma\_frailty\_fit".  
`...` additional graphical parameters.

**Value**

No return value, called for side effects (plotting).

---

plot\_scale\_location     *Scale-Location Plot*

---

**Description**

Plots the square root of absolute deviance residuals against fitted survival probabilities to detect heteroscedasticity.

**Usage**

```
plot_scale_location(fit, ...)
```

**Arguments**

fit                    An object of class "gamma\_frailty\_fit".  
...                    additional graphical parameters.

**Value**

No return value, called for side effects (plotting).

---

plot\_survival\_km        *Kaplan-Meier vs Model-Based Survival Plot*

---

**Description**

Overlays the Kaplan-Meier curve (empirical) with the model-based survival curve evaluated at the mean covariate vector.

**Usage**

```
plot_survival_km(fit, ...)
```

**Arguments**

fit                    An object of class "gamma\_frailty\_fit".  
...                    additional graphical parameters.

**Value**

No return value, called for side effects (plotting).

---

predict\_frailty      *Predictions from a Gamma Frailty Model*

---

### Description

Computes survival probabilities, hazard rates, median survival times, expected survival in a window, risk scores, marginal survival, and forecasted survival curves for a fitted gamma frailty model.

### Usage

```
predict_frailty(
  fit,
  newdata = NULL,
  newtime = NULL,
  type = c("survival", "hazard", "median", "expected", "risk", "marginal", "forecast"),
  window = NULL
)
```

### Arguments

fit	An object of class "gamma_frailty_fit".
newdata	numeric matrix or data frame of covariates for prediction. If NULL the training covariates are used.
newtime	numeric vector of time points for prediction. If NULL the training times are used.
type	character; the type of prediction: "survival" Matrix of survival probabilities (subjects x times). "hazard" Matrix of hazard rates (subjects x times). "median" Numeric vector of median survival times. "expected" Expected survival probability drop in window. "risk" Risk score $\eta_j = \exp(X_j \hat{\beta})$ . "marginal" Marginal survival (population-average, averaged over frailty and observed covariates). "forecast" Extended survival curve beyond the training range; use newtime to specify forecast horizon.
window	numeric vector of length 2 ( $t_1, t_2$ ) giving the time interval for type = "expected".

### Value

Depends on type:

- "survival", "hazard", "forecast": a list with element survival or hazard - a matrix (subjects x times).
- "median": numeric vector (one value per subject).
- "expected": numeric vector (one value per subject).
- "risk": numeric vector of risk scores.
- "marginal": numeric vector of population-average survival at each time in newtime.

**Examples**

```

set.seed(5)
dat <- r_gamma_frailty(100, "pxg", par = c(1, 0.8), theta = 0.4,
  x = matrix(rnorm(200), ncol = 2),
  beta = c(0.3, -0.2),
  cen_type = "right", cen_rate = 0.2)
fit <- fit_gamma_frailty(dat$time, dat$status, dat[, 4:5],
  baseline = "pxg")
# Survival at training times
pred_S <- predict_frailty(fit, type = "survival")
# Median survival
med <- predict_frailty(fit, type = "median")

```

---

residuals\_frailty      *Residuals for the Gamma Frailty Model*

---

**Description**

Computes a comprehensive set of residuals and goodness-of-fit metrics for a fitted gamma frailty model.

**Usage**

```
residuals_frailty(fit)
```

**Arguments**

**fit**                    An object of class "gamma\_frailty\_fit".

**Value**

A named list containing:

**cox\_snell** Cox-Snell residuals  $r_i = -\log S(t_i)$ .

**martingale** Martingale residuals  $M_i = \delta_i - r_i$ .

**deviance** Deviance residuals.

**raw** Raw residuals (model CDF minus empirical CDF on sorted data).

**standardized** Standardized raw residuals.

**studentized** Studentized (leave-one-out approximation) residuals.

**fitted\_S** Fitted survival probabilities.

**MSE, RMSE, MAE** Mean squared / root mean squared / mean absolute error of raw residuals.

**R\_square, Adj\_R\_square** R-squared of model CDF vs empirical CDF.

**KS\_stat, KS\_pvalue** Kolmogorov-Smirnov test statistic and p-value (Cox-Snell residuals vs Exp(1)).

**Examples**

```

set.seed(1)
dat <- r_gamma_frailty(80, "lindley", par = 1.5, theta = 0.5,
                      cen_type = "right", cen_rate = 0.3)
fit <- fit_gamma_frailty(dat$time, dat$status, baseline = "lindley")
res <- residuals_frailty(fit)
plot(res$fitted_S, res$deviance, xlab = "Fitted S(t)", ylab = "Deviance")

```

---

risk\_predict

*Risk Prediction for New Subjects*


---

**Description**

Computes risk scores  $\eta_j = \exp(X_j \hat{\beta})$  and corresponding survival curves for new observations.

**Usage**

```
risk_predict(fit, newdata, times = NULL)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
newdata	numeric matrix or data frame of covariates for new subjects.
times	numeric vector of time points for survival prediction.

**Value**

A list with risk (risk scores) and survival (matrix of survival probabilities, subjects x times).

**Examples**

```

set.seed(4)
dat <- r_gamma_frailty(100, "arvind", par = 0.5, theta = 0.3,
                      x = matrix(rnorm(200), ncol = 2),
                      beta = c(0.4, -0.3),
                      cen_type = "right")
fit <- fit_gamma_frailty(dat$time, dat$status, dat[, 4:5],
                        baseline = "arvind")
new <- matrix(c(1, -0.5, 0.5, 1), nrow = 2)
risk_predict(fit, newdata = new, times = c(0.5, 1, 2))

```

---

r_arvind	<i>Random samples from the Arvind distribution</i>
----------	--

---

**Description**

Generates  $n$  random observations from the Arvind distribution with parameter  $\alpha$  using the inverse-CDF method. The survival function is  $S(t) = \exp(-\alpha t^2)/(1 + \alpha t)$ .

**Usage**

```
r_arvind(n, alpha)
```

**Arguments**

n	integer; number of observations.
alpha	positive numeric; shape/rate parameter.

**Value**

Numeric vector of length  $n$ .

**References**

Pandey, A., Singh, R. P., Tyagi, S., & Tyagi, A. (2024). Modelling climate, COVID-19, and reliability data: A new continuous lifetime model under different methods of estimation. *Stat. Appl.*, 22(2).

**Examples**

```
set.seed(1)
x <- r_arvind(50, alpha = 0.5)
hist(x, main = "Arvind samples")
```

---

r_gamma_frailty	<i>Generate Random Survival Times from the Gamma Frailty Model</i>
-----------------	--

---

**Description**

Generates  $n$  random survival times from the specified gamma frailty model using the inverse-CDF method. Seven censoring mechanisms are supported:

- "none" Complete (uncensored) data.
- "right" Random right censoring with exponential censoring times at rate `cen_rate`.
- "left" Left censoring at a fixed threshold `left_threshold`.
- "interval" Interval censoring with window width `int_width`.

"type1" Type-I (time-terminated) censoring: all subjects observed up to a fixed time `cen_time`; those who have not failed by `cen_time` are right-censored at `cen_time`.

"type2" Type-II (failure-terminated) censoring: the experiment terminates at the `r_failures`-th observed failure; the remaining  $n - r$  subjects are right-censored at that time.

"progressive" Progressive Type-II censoring: at each of the first `length(prog_scheme)` failure times, `prog_scheme[j]` surviving units are randomly withdrawn.

"progressive\_type1" Progressive Type-I censoring: at each pre-specified time in `prog_times`, `prog_scheme[j]` surviving units are randomly withdrawn; the rest are observed until failure.

## Usage

```
r_gamma_frailty(
  n,
  baseline,
  par,
  x = matrix(nrow = n, ncol = 0),
  beta = numeric(0),
  theta,
  cen_type = c("none", "right", "left", "interval", "type1", "type2", "progressive",
    "progressive_type1"),
  cen_rate = 0.2,
  left_threshold = NULL,
  int_width = NULL,
  cen_time = NULL,
  r_failures = NULL,
  prog_scheme = NULL,
  prog_times = NULL
)
```

## Arguments

<code>n</code>	integer; number of subjects.
<code>baseline</code>	character; baseline distribution name. One of "arvind", "lindley", "lfr", "pxg", "mtl", "pfr".
<code>par</code>	numeric vector of true baseline parameters.
<code>x</code>	numeric matrix of covariates (default: no covariates).
<code>beta</code>	numeric vector of true regression coefficients.
<code>theta</code>	positive numeric; true frailty variance.
<code>cen_type</code>	character; censoring mechanism. One of "none", "right", "left", "interval", "type1", "type2", "progressive", "progressive_type1".
<code>cen_rate</code>	positive numeric; exponential censoring rate used for "right" and "progressive" censoring (default 0.2).
<code>left_threshold</code>	numeric; fixed left-censoring threshold (used when <code>cen_type = "left"</code> ). Defaults to the 20th percentile of the true event times.
<code>int_width</code>	positive numeric; width of interval-censoring windows (used when <code>cen_type = "interval"</code> ). Defaults to the 15th percentile of the true event times.

cen_time	positive numeric; fixed censoring time for Type-I censoring (cen_type = "type1"). Defaults to the 70th percentile of the true event times.
r_failures	positive integer; number of failures to observe before terminating the study for Type-II censoring (cen_type = "type2"). Defaults to $\lfloor 0.7n \rfloor$ .
prog_scheme	integer vector; for cen_type = "progressive", the number of units withdrawn at each of the first length(prog_scheme) failure times. For cen_type = "progressive_type1", the number of units withdrawn at each time in prog_times. Defaults to a vector of 1s.
prog_times	positive numeric vector; pre-specified withdrawal times for Progressive Type-I censoring (cen_type = "progressive_type1"). Defaults to the 25th, 50th, and 75th percentiles of the true event times.

### Value

A data frame with columns:

**time** event or censoring time.

**time2** right end of interval (only for cen\_type = "interval", otherwise NA).

**status** 1 = exact event, 0 = right-censored (includes Type-I, Type-II, and progressive withdrawals), 2 = left-censored, 3 = interval-censored.

plus any covariate columns from x.

### Examples

```
set.seed(42)
# Random right censoring
dat <- r_gamma_frailty(n = 100, baseline = "arvind", par = 0.5,
                      theta = 0.3, cen_type = "right", cen_rate = 0.2)
head(dat)

# Type-I censoring (fixed censoring time)
dat_t1 <- r_gamma_frailty(n = 100, baseline = "arvind", par = 0.5,
                         theta = 0.3, cen_type = "type1", cen_time = 2.0)
table(dat_t1$status) # 0 = censored at 2.0, 1 = failed before 2.0

# Type-II censoring (fixed failure count)
dat_t2 <- r_gamma_frailty(n = 100, baseline = "arvind", par = 0.5,
                         theta = 0.3, cen_type = "type2", r_failures = 70L)
table(dat_t2$status) # exactly 70 events (status=1)

# Progressive Type-I censoring
dat_pt1 <- r_gamma_frailty(n = 100, baseline = "arvind", par = 0.5,
                          theta = 0.3, cen_type = "progressive_type1",
                          prog_times = c(1, 2, 3), prog_scheme = c(5L, 5L, 5L))
table(dat_pt1$status)
```

---

`r_lfr`*Random samples from the Linear Failure Rate distribution*

---

**Description**

Generates  $n$  random observations from the Linear Failure Rate (LFR) distribution with parameters  $a$  and  $b$  via the inverse-CDF method. The survival function is  $S(t) = \exp(-at - bt^2/2)$ .

**Usage**

```
r_lfr(n, a, b)
```

**Arguments**

<code>n</code>	integer; number of observations.
<code>a</code>	non-negative numeric; intercept of the hazard.
<code>b</code>	non-negative numeric; slope of the hazard.

**Value**

Numeric vector of length  $n$ .

**References**

Bain, L. J. (1974). Analysis for the linear failure-rate life-testing distribution. *Technometrics*, 16(4), 551-559.

**Examples**

```
set.seed(1)
x <- r_lfr(100, a = 0.5, b = 0.2)
hist(x, main = "LFR samples")
```

---

`r_lindley`*Random samples from the Lindley distribution*

---

**Description**

Generates  $n$  random observations from the Lindley distribution with parameter  $\lambda$  using a mixture representation:  $X \sim p \cdot \text{Exp}(\lambda) + (1 - p) \cdot \text{Gamma}(2, \lambda)$  where  $p = \lambda/(1 + \lambda)$ .

**Usage**

```
r_lindley(n, lambda)
```

**Arguments**

n integer; number of observations.  
lambda positive numeric; rate parameter.

**Value**

Numeric vector of length n.

**References**

Lindley, D. V. (1958). Fiducial distributions and Bayes' theorem. *Journal of the Royal Statistical Society. Series B (Methodological)*, 102-107.

**Examples**

```
set.seed(1)
x <- r_lindley(100, lambda = 1.5)
hist(x, main = "Lindley samples")
```

---

r\_mtl

*Random samples from the Modified Topp-Leone distribution*

---

**Description**

Generates n random observations from the Modified Topp-Leone (MTL) distribution with parameter alpha using the inverse-CDF method via numerical root-finding.

**Usage**

```
r_mtl(n, alpha)
```

**Arguments**

n integer; number of observations.  
alpha positive numeric; shape parameter.

**Value**

Numeric vector of length n.

**References**

Singh, B., Tyagi, S., Singh, R. P., & Tyagi, A. (2025). Modified Topp-Leone distribution: properties, classical and Bayesian estimation with application to COVID-19 and reliability data. *Thailand Statistician*, 23(1), 72-96.

**Examples**

```
set.seed(1)
x <- r_mtl(50, alpha = 2.0)
hist(x, main = "Modified Topp-Leone samples")
```

---

**r\_pfr***Random samples from the Power Failure Rate distribution*

---

**Description**

Generates n random observations from the Power Failure Rate (PFR) distribution with parameters a and k using the closed-form inverse-CDF:  $t = \left( \frac{(k+1)(-\log U)}{a} \right)^{1/(k+1)}$ .

**Usage**

```
r_pfr(n, a, k)
```

**Arguments**

n	integer; number of observations.
a	positive numeric; scale parameter.
k	non-negative numeric; shape parameter ( $k \neq -1$ ).

**Value**

Numeric vector of length n.

**References**

Mugdadi, A. R. (2005). The least squares type estimation of the parameters in the power hazard function. Applied Mathematics and Computation, 169(2), 737-748.

**Examples**

```
set.seed(1)
x <- r_pfr(100, a = 0.5, k = 1.0)
hist(x, main = "Power Failure Rate samples")
```

---

r_pxg	<i>Random samples from the Power Xgamma distribution</i>
-------	--

---

**Description**

Generates  $n$  random observations from the Power Xgamma distribution with parameters  $\alpha$  and  $\beta$  using the inverse-CDF method via numerical root-finding.

**Usage**

```
r_pxg(n, alpha, beta)
```

**Arguments**

n	integer; number of observations.
alpha	positive numeric; first shape parameter.
beta	positive numeric; second shape parameter.

**Value**

Numeric vector of length  $n$ .

**References**

Tyagi, S., Kumar, S., Pandey, A., Saha, M., & Bagariya, H. Power xgamma distribution: Properties and its applications to cancer data. *Int J Stat Reliab Eng.* 2022; 9(1): 51-60.

**Examples**

```
set.seed(1)
x <- r_pxg(50, alpha = 1.0, beta = 0.8)
hist(x, main = "Power Xgamma samples")
```

---

simulate_mle_performance	<i>Quick Simulation Performance Check</i>
--------------------------	---

---

**Description**

A lightweight single-scenario simulation to quickly verify MLE parameter recovery. Prints bias and MSE for each parameter.

**Usage**

```
simulate_mle_performance(  
  n_sim = 100L,  
  n = 100L,  
  baseline = "arvind",  
  par = 0.5,  
  beta = numeric(0),  
  theta = 0.5,  
  cen_rate = 0.1  
)
```

**Arguments**

n_sim	integer; number of replicates (default 100).
n	integer; sample size (default 100).
baseline	character; baseline distribution.
par	numeric vector of true baseline parameters.
beta	numeric vector of true regression coefficients.
theta	positive numeric; true frailty variance.
cen_rate	numeric; exponential censoring rate.

**Value**

A data frame (invisibly) with columns True, Mean, Bias, MSE.

**Examples**

```
set.seed(99)  
simulate_mle_performance(n_sim = 50, n = 80, baseline = "pfr",  
  par = c(0.5, 1), theta = 0.4)
```

---

simulation\_study

*Monte Carlo Simulation Study for Gamma Frailty Models*

---

**Description**

Evaluates MLE performance (bias, MSE, coverage, and convergence rate) for a specified gamma frailty model across multiple sample sizes and censoring settings.

**Usage**

```
simulation_study(
  n_sim = 500L,
  n_vec = c(50L, 100L, 200L),
  baseline = "arvind",
  par = 0.5,
  beta = numeric(0),
  theta = 0.5,
  cen_type = "right",
  cen_rate = 0.2,
  conf_level = 0.95,
  verbose = TRUE
)
```

**Arguments**

<code>n_sim</code>	integer; number of Monte Carlo replicates per scenario (default 500).
<code>n_vec</code>	integer vector; sample sizes to evaluate (default <code>c(50, 100, 200)</code> ).
<code>baseline</code>	character; baseline distribution.
<code>par</code>	numeric vector of true baseline parameters.
<code>beta</code>	numeric vector of true regression coefficients (or <code>numeric(0)</code> for no-covariate models).
<code>theta</code>	positive numeric; true frailty variance.
<code>cen_type</code>	character; censoring type passed to <code>r_gamma_frailty</code> .
<code>cen_rate</code>	positive numeric; censoring rate (for right/progressive).
<code>conf_level</code>	numeric; nominal coverage probability for CIs (default 0.95).
<code>verbose</code>	logical; print progress (default TRUE).

**Value**

A data frame summarising, for each sample size, the mean estimate, bias, MSE, and 95% CI coverage for each parameter.

**Examples**

```
set.seed(42)
sim_res <- simulation_study(
  n_sim = 100, n_vec = c(50, 100),
  baseline = "arvind", par = 0.5,
  beta = 0.5, theta = 0.3,
  cen_type = "right", cen_rate = 0.2
)
print(sim_res)
```

---

survival_at	<i>Survival Probability at Specified Time Points</i>
-------------	--

---

**Description**

Returns a tidy data frame of predicted survival probabilities at user-supplied time points, one row per (subject, time) combination.

**Usage**

```
survival_at(fit, times, newdata = NULL)
```

**Arguments**

fit	An object of class "gamma_frailty_fit".
times	numeric vector of time points.
newdata	optional covariate matrix / data frame for new subjects.

**Value**

A data frame with columns subject, time, survival.

**Examples**

```
set.seed(1)
dat <- r_gamma_frailty(60, "arvind", par = 0.5, theta = 0.3,
                      cen_type = "right")
fit <- fit_gamma_frailty(dat$time, dat$status, baseline = "arvind")
survival_at(fit, times = c(0.5, 1, 2))
```

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