

# Package ‘CopulaInference’

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**Type** Package

**Title** Estimation and Goodness-of-Fit of Copula-Based Models with Arbitrary Distributions

**Version** 0.5.0

**Description** Estimation and goodness-of-fit functions for copula-based models of bivariate data with arbitrary distributions (discrete, continuous, mixture of both types). The copula families considered here are the Gaussian, Student, Clayton, Frank, Gumbel, Joe, Plackett, BB1, BB6, BB7, BB8, together with the following non-central squared copula families in Nasri (2020) <[doi:10.1016/j.spl.2020.108704](https://doi.org/10.1016/j.spl.2020.108704)>: ncs-gaussian, ncs-clayton, ncs-gumbel, ncs-frank, ncs-joe, and ncs-plackett. For theoretical details, see, e.g., Nasri and Remillard (2023) <[arXiv:2301.13408](https://arxiv.org/abs/2301.13408)>.

**License** GPL-3

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**Index****23***AuxFun**Auxiliary functions***Description**

This function computes the empirical margins, their left-limits, Kendall's tau and Spearman's rho for arbitrary data. Slower than AuxFunC based on C.

**Usage**

```
AuxFun(data)
```

**Arguments**

data	Matrix (x,y) of size n x 2
------	----------------------------

**Value**

tau	Kendall's tau
rho	Spearman's rho
Fx	Empirical cdf of x
Fxm	Left-limit of the empirical cdf of x
Fy	Empirical cdf of y
Fym	Left-limit of the empirical cdf of y

## References

- Nasri (2022). Test of serial dependence for arbitrary distributions. JMVA  
 Nasri & Remillard (2023). Tests of independence and randomness for arbitrary data using copula-based covariances, arXiv 2301.07267.

## Examples

```
data(simgumbel)
out=AuxFun(simgumbel)
```

## Description

This function computes the empirical margins, their left-limits, Kendall's tau and Spearman's rho for arbitrary data

## Usage

```
AuxFunC(data)
```

## Arguments

data	Matrix (x,y) of size n x 2
------	----------------------------

## Value

tau	Kendall's tau
rho	Spearman's rho
Fx	Empirical cdf of x
Fxm	Left-limit of the empirical cdf of x
Fy	Empirical cdf of y
Fym	Left-limit of the empirical cdf of y

## References

- Nasri (2022). Test of serial dependence for arbitrary distributions. JMVA  
 Nasri & Remillard (2023). Tests of independence and randomness for arbitrary data using copula-based covariances, arXiv 2301.07267.

**Examples**

```
data(simgumbel)
out=AuxFunC(simgumbel)
```

**BiEmpCdf***Empirical bivariate cdf***Description**

This function computes the empirical joint cdf evaluated at all points (y1,y2)

**Usage**

```
BiEmpCdf(data, y1, y2)
```

**Arguments**

data	Matrix (x1,x2) of size n x 2
y1	Vector of size n1
y2	Vector of size n2

**Value**

cdf	Empirical cdf
-----	---------------

**Examples**

```
data(simgumbel)
out=BiEmpCdf(simgumbel,c(0,1),c(-1,0,1))
```

**CdfInv***Quantile function***Description**

This function computes the inverse of the cdf of a finite distribution for a vector of probabilities.

**Usage**

```
CdfInv(u, y, Fn)
```

**Arguments**

u	Vector of probabilities
y	Ordered values
Fn	Cdf

**Value**

x	Vector of quantiles
---	---------------------

**Examples**

```
y=c(0,1,2)
Fn = c(0.5,0.85,1)
out=CdfInv(c(1:9)/10,y,Fn)
```

dnncs

*Density of non-central squared copula***Description**

This function computes the density of the non-central squared copula (nccs) associated with a one-parameter copula with parameter cpar, and parameters a1, a2 >0 .

**Usage**

```
dnncs(data, family, rotation = 0, par)
```

**Arguments**

data	Matrix (x,y) of size n x 2
family	Copula family: "nccs-gaussian", "nccs-clayton", "nccs-frank", "nccs-gumbel", "nccs-joe", "nccs-plackett".
rotation	Rotation: 0 (default value), 90, 180, or 270.
par	vector of copula parameter and non-centrality parameter a1,a2 >0

**Value**

pdf	Density
-----	---------

**References**

Nasri (2020). On non-central squared copulas. Statistics and Probability Letters.

**Examples**

```
dncs(c(0.5,0.8),"ncs-clayton",par=c(2,1,2))
```

dplac	<i>Density of Plackett copula</i>
-------	-----------------------------------

**Description**

This function computes the density of the Plackett copula with parameter par>0.

**Usage**

```
dplac(data, rotation = 0, par)
```

**Arguments**

data	Matrix (x,y) of size n x 2
rotation	Rotation: 0 (default value), 90, 180, or 270.
par	Copula parameter >0

**Value**

pdf	Density
-----	---------

**Examples**

```
dplac(c(0.5,0.8),par=3,rotation=270)
```

EmpCdf	<i>Empirical univariate cdf</i>
--------	---------------------------------

**Description**

This function computes the empirical cdf evaluated at all sample points

**Usage**

```
EmpCdf(x)
```

**Arguments**

x	Observations
---	--------------

**Value**

$F_x$	Empirical cdf
$F_{xm}$	Left limit of the empirical cdf
$I_x$	Indicator of atoms



**Examples**

```
data(simgumbel)
out=EmpCdf(simgumbel[,1])
```

EstBiCop

*Parameter estimation for bivariate copula-based models with arbitrary distributions*

**Description**

Computes the estimation of the parameters of a copula-based model with arbitrary distributions, i.e, possibly mixtures of discrete and continuous distributions. Parametric margins are allowed. The estimation is based on a pseudo-likelihood adapted to ties.

**Usage**

```
EstBiCop(
  data = NULL,
  family,
  rotation = 0,
  Fx = NULL,
  Fxm = NULL,
  Fy = NULL,
  Fym = NULL
)
```

**Arguments**

<code>data</code>	Matrix or data frame with 2 columns (X,Y). Can be pseudo-observations. If NULL, $F_x$ and $F_y$ must be provided.
<code>family</code>	Copula family: "gaussian", "t", "clayton", "frank", "gumbel", "joe", "plackett", "bb1", "bb6", "bb7", "bb8", "ncs-gaussian", "ncs-clayton", "ncs-gumbel", "ncs-frank", "ncs-joe", "ncs-plackett".
<code>rotation</code>	Rotation: 0 (default value), 90, 180, or 270.
<code>Fx</code>	Marginal cdf function applied to X (default is NULL).
<code>Fxm</code>	Left-limit of marginal cdf function applied to X default is NULL).
<code>Fy</code>	Marginal cdf function applied to Y (default is NULL).
<code>Fym</code>	Left-limit of marginal cdf function applied to Y (default is NULL).

**Value**

<code>par</code>	Copula parameters
<code>family</code>	Copula family
<code>rotation</code>	Rotation value
<code>tauth</code>	Kendall's tau corresponding to the estimated parameter
<code>tauemp</code>	Empirical Kendall's tau (from the multilinear empirical copula)
<code>rhoSth</code>	Spearman's rho corresponding to the estimated parameter
<code>rhoSemp</code>	Empirical Spearman's tau (from the multilinear empirical copula)
<code>loglik</code>	Log-likelihood
<code>aic</code>	Aic value
<code>bic</code>	Bic value
<code>data</code>	Matrix of values (could be (Fx,Fy))
<code>F1</code>	Cdf of X (Fx if provided, empirical otherwise)
<code>F1m</code>	Left-limit of F1 (Fxm if provided, empirical otherwise)
<code>F2</code>	Cdf of Y (Fy if provided, empirical otherwise)
<code>F2m</code>	Left-limit of F2 (Fym if provided, empirical otherwise)
<code>ccdfx</code>	Conditional cdf of X given Y and its left limit
<code>ccdfxm</code>	Left-limit of ccdfx
<code>ccdfy</code>	Conditional cdf of Y given X and its left limit
<code>ccdfym</code>	Left-limit of ccdfy

**References**

Nasri & Remillard (2023). Identifiability and inference for copula-based semiparametric models for random vectors with arbitrary marginal distributions. arXiv 2301.13408.

Nasri (2020). On non-central squared copulas. Statistics and Probability Letters.

**Examples**

```
set.seed(2)
data = matrix(rpois(20,1),ncol=2)
out0=EstBiCop(data,"gumbel")
```

---

EstDep	<i>Kendall's tau and Spearman's rho</i>
--------	---

---

**Description**

This function computes Kendall's tau and Spearman's rho for arbitrary data. These are invariant by increasing mappings.

**Usage**

```
EstDep(data)
```

**Arguments**

data	Matrix or data frame with 2 columns (X,Y). Can be pseudo-observations.
------	--

**Value**

tau	Kendall's tau
rho	Spearman's rho

**References**

Nasri (2022). Test of serial dependence for arbitrary distributions. JMVA

Nasri & Remillard (2023). Tests of independence and randomness for arbitrary data using copula-based covariances, arXiv 2301.07267.

**Examples**

```
data(simgumbel)
out=EstDep(simgumbel)
```

---

est_options	<i>Options for the estimation of the parameters of bivariate copula-based models</i>
-------------	--

---

**Description**

Sets starting values, upper and lower bounds for the parameters. The bounds are based on those in the rvinecopulib package.

**Usage**

```
est_options(family, tau = 0.5)
```

**Arguments**

<code>family</code>	Copula family: "gaussian", "t", "clayton", "frank", "gumbel", "joe", "plackett", "bb1", "bb6", "bb7", "bb8", "ncs-gaussian", "ncs-clayton", "ncs-gumbel", "ncs-frank", "ncs-joe", "ncs-plackett".
<code>tau</code>	Estimated Kendall's tau to compute a starting point (default is 0.5)

**Value**

<code>LB</code>	Lower bound for the parameters
<code>UB</code>	Upper bound for the parameters
<code>start</code>	Starting point for the estimation

**References**

- Nagler & Vatter (2002). *rvinecopulib*: High Performance Algorithms for Vine Copula Modeling. Version 0.6.2.1.3
- Nasri (2020). On non-central squared copulas. *Statistics and Probability Letters*.
- Nasri (2022). Test of serial dependence for arbitrary distributions. *JMVA*.
- Nasri & Remillard (2023). Copula-based dependence measures for arbitrary data, arXiv 2301.07267.

**Examples**

```
out = est_options("bb8")
```

**Finv***Quantile function of margins***Description**

This function computes the quantile of seven cdf used in Nasri (2022).

**Usage**

```
Finv(u, k)
```

**Arguments**

<code>u</code>	Vector of probabilities
<code>k</code>	Marginal distribution: [1] Bernoulli(0.8), [2] Poisson(6), [3] Negative binomial with r = 1.5, p = 0.2, [4] Zero-inflated Poisson (10) with w = 0.1 and P(6.67) otherwise, [5] Zero-inflated Gaussian, [6] Discretized Gaussian, [7] Discrete Pareto(1)

**Value**

x Vector of quantiles

**Author(s)**

Bouchra R. Nasri January 2021

**References**

B.R Nasri (2022). Tests of serial dependence for arbitrary distributions

**Examples**

```
x = Finv(runif(40),2)
```

---

fnumber

*Family number corresponding to VineCopula package*

---

**Description**

Computes the number associated with a copula family (without rotation)

**Usage**

```
fnumber(family)
```

**Arguments**

family Copula family: "gaussian", "t", "clayton", "frank", "gumbel", "joe", "plackett", "bb1", "bb6", "bb7", "bb8".

**Value**

fnumber Number

**References**

Nagler et al. (2023). VineCopula: Statistical Inference of Vine Copulas, version 2.4.5.

**Examples**

```
fnumber("bb1")
```

## Description

Goodness-of-fit tests for copula-based models for data with arbitrary distributions. The tests statistics are the Cramer-von Mises statistic ( $S_n$ ), the difference between the empirical Kendall's tau and the theoretical one, and the difference between the empirical Spearman's rho and the theoretical one.

## Usage

```
GofBiCop(
  data = NULL,
  family,
  rotation = 0,
  Fx = NULL,
  Fxm = NULL,
  Fy = NULL,
  Fym = NULL,
  B = 100,
  n_cores = 1
)
```

## Arguments

<code>data</code>	Matrix or data frame with 2 columns (X,Y). Can be pseudo-observations. If NULL, <code>Fx</code> and <code>Fy</code> must be provided.
<code>family</code>	Copula family: "gaussian", "t", "clayton", "frank", "gumbel", "joe", "plackett", "bb1", "bb6", "bb7", "bb8", "ncs-gaussian", "ncs-clayton", "ncs-gumbel", "ncs-frank", "ncs-joe", "ncs-plackett".
<code>rotation</code>	Rotation: 0 (default value), 90, 180, or 270.
<code>Fx</code>	marginal cdf function applied to X (default is NULL).
<code>Fxm</code>	left limit of marginal cdf function applied to X default is NULL).
<code>Fy</code>	marginal cdf function applied to Y (default is NULL).
<code>Fym</code>	left limit of marginal cdf function applied to Y (default is NULL).
<code>B</code>	Number of bootstrap samples (default 100)
<code>n_cores</code>	Number of cores to be used for parallel computing (default is 1).

## Value

<code>pvalueSn</code>	Pvalue of $S_n$ in percent
<code>pvalueTn</code>	Pvalue of $T_n$ in percent

pvalueRn	Pvalue of Rn in percent
Sn	Value of Cramer-von Mises statistic Sn
Tn	Value of Kendall's statistic Tn
Rn	Value of Spearman's statistic Rn
cpar	Copula parameters
family	Copula family
rotation	Rotation value
tauth	Kendall's tau (from the multilinear theoretical copula)
tauemp	Empirical Kendall's tau (from the multilinear empirical copula)
rhoth	Spearman's rho (from the multilinear theoretical copula)
rhoemp	Empirical Spearman's rho (from the multilinear empirical copula)
parB	Bootstrapped parameters
loglik	Log-likelihood
aic	AIC value
bic	BIC value

## References

- Nasri & Remillard (2023). Identifiability and inference for copula-based semiparametric models for random vectors with arbitrary marginal distributions. arXiv 2301.13408.
- Nasri & Remillard (2023). Goodness-of-fit and bootstrapping for copula-based random vectors with arbitrary marginal distributions.
- Nasri (2020). On non-central squared copulas. Statistics and Probability Letters.

## Examples

```
data = rvinecopulib::rbicop(10, "gumbel", rotation=0, 2)
out=GofBiCop(data, family="gumbel", B=10)
```

## Description

This function computes the conditional distribution of the non-central squared copula (ncs) associated with a one-parameter copula with parameter cpar, and parameters a1, a2 >0 .

## Usage

```
hnscs(data, cond_var, family, rotation = 0, par)
```

**Arguments**

<code>data</code>	Matrix (x,y) of size n x 2
<code>cond_var</code>	Conditioning variable (1 or 2)
<code>family</code>	Copula family: "ncs-gaussian", "ncs-clayton", "ncs-frank", "ncs-gumbel", "ncs-joe", "ncs-plackett".
<code>rotation</code>	Rotation: 0 (default value), 90, 180, or 270.
<code>par</code>	vector of copula parameter and non-centrality parameter a1,a2 >0

**Value**

<code>h</code>	Conditional cdf
----------------	-----------------

**References**

Nasri (2020). On non-central squared copulas. Statistics and Probability Letters.

**Examples**

```
hncs(c(0.5,0.8),1,"ncs-clayton",270,c(2,1,2))
```

`hplac`

*Conditional distribution of Plackett copula*

**Description**

This function computes the conditional distribution of the Plackett copula with parameter `par`>0.

**Usage**

```
hplac(data, cond_var, rotation = 0, par)
```

**Arguments**

<code>data</code>	Matrix (x,y) of size n x 2
<code>cond_var</code>	Conditioning variable (1 or 2)
<code>rotation</code>	Rotation: 0 (default value), 90, 180, or 270.
<code>par</code>	Copula parameter >0

**Value**

<code>h</code>	Conditional cdf
----------------	-----------------

## Examples

```
hplac(c(0.5,0.8),1,270,3)
```

identifiability	<i>Identifiability of two-parameter copula families</i>
-----------------	---

## Description

Determines if a copula family is identifiable with respect to the empirical margins. One-parameter copula families ("gaussian", "gumbel", "clayton", "frank", "plackett", "joe") are identifiable whatever the margins. The rank of the gradient of the copula on the range of the margins is evaluated at 10000 parameter points within the lower and upper bounds of the copula family.

## Usage

```
identifiability(data = NULL, family, rotation = 0, Fx = NULL, Fy = NULL)
```

## Arguments

data	Matrix or data frame with 2 columns (X,Y). Can be pseudo-observations. If NULL, Fx and Fy must be provided.
family	Copula family: "gaussian", "t", "clayton", "frank", "gumbel", "joe", "plackett", "bb1", "bb6", "bb7", "bb8", "ncs-gaussian", "ncs-clayton", "ncs-gumbel", "ncs-frank", "ncs-joe", "ncs-plackett".
rotation	Rotation: 0 (default value), 90, 180, or 270.
Fx	Marginal cdf function applied to X (default is NULL).
Fy	Marginal cdf function applied to Y (default is NULL).

## Value

out	True or False
-----	---------------

## References

- Nasri & Remillard (2023). Identifiability and inference for copula-based semiparametric models for random vectors with arbitrary marginal distributions. arXiv 2301.13408.
- Nasri (2020). On non-central squared copulas. Statistics and Probability Letters.

## Examples

```
set.seed(1)
data = matrix(rpois(20,1),ncol=2)
out = identifiability(data,"gumbel")
```

---

<code>pncs</code>	<i>Cdf for non-central squared copula</i>
-------------------	---

---

### Description

This function computes the distribution function of the non-central squared copula (ncs) associated a with one-parameter copula with parameter cpar, and parameters a1, a2 >0 .

### Usage

```
pncs(data, family, rotation = 0, par)
```

### Arguments

<code>data</code>	Matrix (x,y) of size n x 2
<code>family</code>	Copula family: "ncs-gaussian", "ncs-clayton", "ncs-frank", "ncs-gumbel", "ncs-joe", "ncs-plackett".
<code>rotation</code>	Rotation: 0 (default value), 90, 180, or 270.
<code>par</code>	vector of copula parameter and non-centrality parameter a1,a2 >0

### Value

<code>cdf</code>	Value of cdf
------------------	--------------

### References

Nasri (2020). On non-central squared copulas. Statistics and Probability Letters.

### Examples

```
pncs(c(0.5,0.8),"ncs-clayton", par=c(2,1,2),rotation=270)
```

---

<code>pplac</code>	<i>Cdf for Plackett copula</i>
--------------------	--------------------------------

---

### Description

This function computes the distribution function of the Plackett copula with parameter par>0.

### Usage

```
pplac(data, rotation = 0, par)
```

**Arguments**

data	Matrix (x,y) of size n x 2
rotation	Rotation: 0 (default value), 90, 180, or 270.
par	Copula parameter >0

**Value**

cdf	Value of cdf
-----	--------------

**Examples**

```
pplac(c(0.5,0.8),270,3)
```

preparedata	<i>Computes unique values, cdf and pdf</i>
-------------	--

**Description**

This function computes the unique values, cdf and pdf for a series of data.

**Usage**

```
preparedata(x)
```

**Arguments**

x	Vector
---	--------

**Value**

values	Unique (sorted) values
m	Number of unique values
Fn	Empirical cdf of the unique values
fn	Empirical pdf of the unique values

**References**

B.R. Nasri (2022). Tests of serial dependence for arbitrary distributions

C. Genest, J.G. Neslehova, B.N. Remillard and O. Murphy (2019). Testing for independence in arbitrary distributions.

```
#' @examples x = c(0,0,0,2,3,1,3,1,2,0) out = prepare_data(x)
```

**rhoplackett***Spearman's rho for Plackett copula***Description**

Computes the theoretical Spearman's rho for Plackett copula

**Usage**

```
rhoplackett(cpar, rotation = 0)
```

**Arguments**

- |          |   |
|----------|---|
| cpar     | Copula parameter; can be a vector.            |
| rotation | Rotation: 0 (default value), 90, 180, or 270. |

**Value**

- |     |                |
|-----|----------------|
| rho | Spearman's rho |
|-----|----------------|

**References**

Remillard (2013). Statistical Methods for Financial Engineering. CRC Press

**Examples**

```
rhoplackett(3,rotation=90)
```

**rnscs***Simulation of non-central squared copula***Description**

This function computes generates a bivariate sample from a non-central squared copula (ncs) associated with a one-parameter copula with parameter cpar, and parameters a1, a2 > 0 .

**Usage**

```
rnscs(n, family, rotation = 0, par)
```

**Arguments**

n	Number of observations
family	Copula family: "ncs-gaussian", "ncs-clayton", "ncs-frank", "ncs-gumbel", "ncs-joe", "ncs-plackett".
rotation	Rotation: 0 (default value), 90, 180, or 270.
par	vector of copula parameter and non-centrality parameter a1,a2 >0

**Value**

U	Observations
---	--------------

**References**

Nasri (2020). On non-central squared copulas. Statistics and Probability Letters.

**Examples**

```
rncs(100,"ncs-clayton",par=c(2,1,2))
```

rplac

*Generates observations from the Plackett copula*

**Description**

This function generates observations from a Plackett copula with parameter par>0.

**Usage**

```
rplac(n, rotation = 0, par)
```

**Arguments**

n	Number of pairs to be generated
rotation	Rotation: 0 (default value), 90, 180, or 270.
par	Copula parameter >0

**Value**

U	Matrix of observations
---	------------------------

**Examples**

```
rplac(10,rotation=90,par=2)
```

**simgumbel***Simulated data***Description**

Simulated data from a Gumbel copula with parameter 2, Bernoulli margin for X1 and zero-inflated Gaussian margin for X2.

**Usage**

```
data(simgumbel)
```

**Format**

Data frame of numerical values

**Examples**

```
data(simgumbel)
plot(simgumbel,xlab="X1", ylab="X2")
```

**statcvm***Goodness-of-fit statistics***Description**

Computation of goodness-of-fit statistics (Cramer-von Mises and the Kendall's tau)

**Usage**

```
statcvm(object)
```

**Arguments**

**object** Object of class ‘EstBiCop’.

**Value**

Sn	Cramer-von Mises statistic
Tn	Kendall's statistic
Rn	Spearman's statistic
tauemp	Empirical Kendall's tau
tauth	Kendall's tau of the multilinear theoretical copula
rhoemp	Empirical Spearman's rho

rhoth	Spearman's rho of the multilinear theoretical copula
Y1	Ordered observed values of X1
F1	Empirical cdf of Y1
Y2	Ordered observed values of X2
F2	Empirical cdf of Y2
cpar	Copula parameters
family	Copula family
rotation	Rotation value
n	Sample size

## References

Nasri & Remillard (2023). Identifiability and inference for copula-based semiparametric models for random vectors with arbitrary marginal distributions. arXiv 2301.13408.

## Examples

```
set.seed(2)
data = matrix(rpois(20,1),ncol=2)
out0 = EstBiCop(data,"gumbel")
out = statcvm(out0)
```

taucop

*Kendall's tau for a copula family*

## Description

This function computes Kendall's tau for a copula family

## Usage

```
taucop(family_number, cpar, rotation = 0)
```

## Arguments

family_number	Integer from 1 to 10
cpar	Copula parameters
rotation	Rotation: 0 (default value), 90, 180, or 270.

## Value

tau	Kendall's tau
-----	---------------

**Examples**

```
taucop(4,2,270) # Gumbel copula
```

**tauplackett**

*Kendall's tau for Plackettfamily*

**Description**

This function computes Kendall's tau for Plackett family using numerical integration

**Usage**

```
tauplackett(cpar, rotation = 0)
```

**Arguments**

cpar	Copula parameter >0
rotation	Rotation: 0 (default value), 90, 180, or 270.

**Value**

tau	Kendall's tau
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**Examples**

```
tauplackett(2,270)
```

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